

General Certificate of Education (A-level) January 2012

Mathematics

MM1B

(Specification 6360)

Mechanics 1B

Final

Mark Scheme

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Key to mark scheme abbreviations

M	mark is for method
m or dM	mark is dependent on one or more M marks and is for method
A	mark is dependent on M or m marks and is for accuracy
В	mark is independent of M or m marks and is for method and accuracy
E	mark is for explanation
√or ft or F	follow through from previous incorrect result
CAO	correct answer only
CSO	correct solution only
AWFW	anything which falls within
AWRT	anything which rounds to
ACF	any correct form
AG	answer given
SC	special case
OE	or equivalent
A2,1	2 or 1 (or 0) accuracy marks
–x EE	deduct x marks for each error
NMS	no method shown
PI	possibly implied
SCA	substantially correct approach
c	candidate
sf	significant figure(s)
dp	decimal place(s)

No Method Shown

Where the question specifically requires a particular method to be used, we must usually see evidence of use of this method for any marks to be awarded.

Where the answer can be reasonably obtained without showing working and it is very unlikely that the correct answer can be obtained by using an incorrect method, we must award **full marks**. However, the obvious penalty to candidates showing no working is that incorrect answers, however close, earn **no marks**.

Where a question asks the candidate to state or write down a result, no method need be shown for full marks.

Where the permitted calculator has functions which reasonably allow the solution of the question directly, the correct answer without working earns **full marks**, unless it is given to less than the degree of accuracy accepted in the mark scheme, when it gains **no marks**.

Otherwise we require evidence of a correct method for any marks to be awarded.

Q	Solution	Marks	Total	Comments
1	7(3i + 8j) + 3(6i - 5j) = 10v	M1A1		M1: Three term equation for conservation
	$\mathbf{v} = 3.9\mathbf{i} + 4.1\mathbf{j}$	A1	3	of momentum with addition of terms and total mass of 10. Allow one error, for
		111		example switching masses or omitting
				negative sign in velocity.
				A1: Correct equation for velocity.
				A1: Correct velocity. Accept $\begin{bmatrix} 3.9 \\ 4.1 \end{bmatrix}$
				Finding speed as 5.66 without showing velocity scores M1 A0 A0
				Finding speed after having correct velocity should be considered as further
				work and not penalised.
				Note: For consistent use of weight deduct one mark.
2(-)	Total		3	D1. Come at force diagram with force
2(a)	$rac{}{}$ R (or 39.2 or N or $4g$)			B1: Correct force diagram with four forces with arrows and labels.
	For μR or μN			Accept words eg friction instead of letters
	50			Ignore negative signs in labels. Do not accept 4 kg for the weight.
	ψ mg or W or 4g or 39.2			Award marks if forces are drawn on the
	mg of W of 4g of 37.2	B1	1	diagram in the question.
(b)	39.2 N	B1	1	B1: Correct reaction force. Accept 4 <i>g</i> . Do not accept 39.
(c)	$50 - F = 4 \times 3$	M1A1		M1: Three term equation of motion with
	F = 38	A1	3	the correct terms.
		AI	3	A1: Correct equation with correct signs. A1: Correct friction.
(d)	$38 = \mu \times 39.2$	M1		M1: Use of $F = \mu R$ with their answers to
	$\mu = \frac{38}{39.2} = 0.969$	A1F	2	(b) and (c).
	39.2	1111	_	A1F: Correct μ based on their answers to (b) and (c). Accept AWRT 0.969.
				Note: $F = 12$ leads to 0.306 and award
				M1 A1F Condone 0.97 or FT to 2sf
				Condone use of inequalities.
(e)	Less friction, so a smaller coefficient of	B1		B1: Less friction.
	friction.	B1	2	B1: Smaller μ .
				Note:
				More friction anywhere scores B0 B0 Less friction, greater μ scores B1 B0
			-	Smaller μ with no/inexact reason B0 B1
	Total		9	

Q	Solution	Marks	Total	Comments
3(a)	$s_1 = \frac{1}{2} \times 5 \times 28 = 70 \text{ m}$	M1A1	2	M1: For $\frac{1}{2} \times 5 \times 28$ or equivalent. A1: Correct distance.
(b)	$s = 70 + \frac{1}{2} \times 5 \times 22$ $= 70 + 55$	B1M1		B1: For $\pm \frac{1}{2} \times 5 \times 22$ or equivalent.
	= 70 + 55 = 125 m	A1F	3	M1: For adding the distances. A1F: Correct distance. Follow through their answer from part (a) only.
(c)	Average speed = $\frac{125}{50}$ = 2.5 ms ⁻¹	M1 A1F	2	M1: For their answer to (b) divided by 50. A1F: Correct average speed. Follow through answers from part (b).
(d)	Displacement from $O = 70 - 55$ = 15 m	B1	1	B1: Correct displacement.
(e)	Average velocity = $\frac{15}{50}$ = 0.3 ms ⁻¹	M1 A1F	2	M1: For their answer to (d) divided by 50, provided they have subtracted in (d). A1F: Correct average velocity. Follow through answers from part (d) Award no marks if the final answer is 0.
(f)	$a = \frac{5}{18} = 0.278 \text{ m s}^{-2}$	B1	1	B1: Correct acceleration. Accept $\frac{5}{18}$ or equivalent fraction or 0.277 or AWRT 0.278. Condone 0.28
	Total		11	

Q	Solution	Marks	Total	Comments
4(a)	$V\sin 30^{\circ} = 3$	M1A1		M1: Resolving parallel to the bank.
	3			Accept $V \cos 30^{\circ} = 3$.
	$V = \frac{3}{\sin 30^\circ} = 6$	A1	3	A1: Correct equation.
	SIII 30°			A1: Correct <i>V</i> .
(h)	200	M1		M1. 200 divided by Win 600 an
(b)	$t = \frac{200}{6\sin 60^{\circ}} = 38 \text{ (seconds)}$	A1F		M1: 200 divided by $V \sin 60^{\circ}$ or $V \sin 30^{\circ}$ or equivalent with their value for
	6 sin 60°	A1F	3	V from (a).
		1111		A1F: Correct expression for t .
				A1F: Correct value for <i>t</i> to nearest second.
	OR			Follow through their answer to part (a)
		0.41		
	$h = \frac{200}{\sin 60^{\circ}} = 230.94$	(M1)		M1:Distance divided by corresponding
		(A1F) (A1F)		velocity.
	$t = \frac{230.94}{6} = 38 \text{ (seconds)}$	(AII')		A1F: Correct expression for <i>t</i> A1F: Correct value for <i>t</i> to nearest second.
	U			Follow through their answer to part (a)
	OR			5
	resultant velocity = $\sqrt{27}$	(M1)		Do not accept 38.5
	$t = \frac{200}{\sqrt{27}} = 38 \text{ (seconds)}$	(A1F)		
	$t = \frac{\sqrt{27}}{\sqrt{27}}$ – 38 (seconds)	(A1F)		
	Total		6	
5(a)	$4720 - 3R = 2200 \times 1.6$	M1A1		M1: Three term horizontal equation of
	_ 4720 – 3520	A1		motion with mass of 2200 kg and $3R$ (or
	$R = \frac{4720 - 3520}{3} = 400$	A1	4	2R and R).
	5			A1: All terms correct (4720, $3R$ and 2200×1.6).
				A1: Correct signs.
	OR			A1: Correct value for <i>R</i> .
	$4720 - R - T = 1200 \times 1.6$	(3.41.4.1)		
		(M1A1) (A1)		M1: Forming an equation for each body
	$T - 2R = 1000 \times 1.6$	(A1)		and adding to eliminate <i>T</i> . A1: Two correct equations.
	4720 - 3R = 3520	,		A1: Correct equation in <i>R</i> .
	R = 400			A1: Correct value for <i>R</i> .
(b)	$T - 2 \times 400 = 1000 \times 1.6$	M1A1F		M1: Three term equation of motion for
	T = 800 + 1600 = 2400 N	A 117	2	caravan with T , $2R$ and 1000×1.6 .
		A1F	3	A1F: Correct equation, with their value
	OR			for <i>R</i> from part (a). A1F: Correct tension. Follow through
				from part (a) using $T = 1600 + 2R$
	4720 T 400 = 1200 × 1 6			r (y)
	$4720 - T - 400 = 1200 \times 1.6$	(M1)		M1: Four term equation of motion for car
	T = 4720 - 400 - 1920 = 2400 N	(A1F)		with 4720, T , R and 1200×1.6 .
		(A1F)		A1F: Correct equation, with their value
				for <i>R</i> from part (a) A1F: Correct tension. Follow through
				from part (a) using $T = 2800 - R$
				Note: do not follow through if a negative
				value is used for R .
	Total		7	

Q	Solution	Marks	Total	Comments
6(a)(i)	$10^2 = 4^2 + 2 \times a \times 50$	M1A1		M1: Use of a constant acceleration
	$a = \frac{100 - 16}{100} = 0.84 \text{ m/s}^{-2}$	A1	3	equation to find a, with v and u substituted correctly.
	100			For example $4^2 = 10^2 + 100a$ scores
				M0A0A0. A1: Correct constant acceleration
				equation.
				A1: Correct a.
				Note if <i>t</i> found first award M1 for use of
				$v = u + at \text{ or } s = ut + \frac{1}{2}at^2.$
				2
(ii)	$50 - \frac{1}{4}(4 + 10)t$	M1A1		M1: Use of a constant acceleration
	$50 = \frac{1}{2}(4+10)t$			equation to find <i>t</i> . A1F: Correct constant acceleration
	$t = \frac{50}{7} = 7.14 \mathrm{s}$	A1	3	equation with their acceleration from
	7			(a)(i) seen.
	OR			A1: Correct t. Accept $\frac{50}{7}$ or $7\frac{1}{7}$ or
	10 = 4 + 0.84t			AWRT 7.14.
		(M1A1F)		If <i>t</i> has been found in part (a) the working
	$t = \frac{6}{0.84} = 7.14 \mathrm{s}$	(A1)		does not have to be repeated, but value of <i>t</i> must be stated.
	OR			
	OK			Do not follow through incorrect values of <i>a</i> .
	$50 = 4t + \frac{1}{2} \times 0.84t^2$	(M1A1F)		u.
	$0.42t^2 + 4t - 50 = 0$			
	t = 7.14 (or $t = -16.6$)	(A1)		
(b)	$70 \times 0.84 = 58.8 \text{ N}$	M1A1F	2	M1: Use of $F = ma$ with $m = 70$ and their a from (a)(i).
				A1F: Correct F. Follow through their
				value of a from part (a)(i).
(c)(i)	$58.8 = 70 \times 9.8 \sin \alpha$	M1A1F		M1: Resolving parallel to the slope must
	$\sin \alpha = \frac{58.8}{70 \times 9.8} = 0.08571$			see 70g or mg OE with $\sin \alpha$ or $\cos \alpha$ and their answer to part (b).
				A1F: Correct equation. Follow through
	$\alpha = 4.92^{\circ}$	A1F	3	their answer to part (b) provided $\sin \alpha < 1$ A1F: Correct angle. Follow through their
				answer to part (b). Accept 4.91° provided
				$\sin \alpha < 1$.

Q	Solution	Marks	Total	Comments
6(c)(ii)	$70 \times 9.8 \sin \alpha - 30 = 58.8$	M1A1F		M1: Three term equation of motion. must
	$\sin \alpha = 0.12945$			see 70 g or mg OE with sin α or cos α . A1F: Correct equation. Follow through
	$\alpha = 7.44^{\circ}$	A1F	3	their answer to part (b) provided $\sin \alpha < 1$ A1F: Correct angle. Follow through their answer to part (b) provided $\sin \alpha < 1$. Accept 7.43°. Accept 7.41° from 0.129.
(d)	The air resistance force will increase (vary or change) with speed.	B1	1	B1: Correct statement.
	Total		15	

Q	Solution	Marks	Total	Comments
7(a)	$h = \frac{1}{2} \times 2.5 \times 20^2$ $= 500 \text{ m}$	M1 A1A1	3	M1: Expression for height or position vector at $t = 20$. A1: Correct expression for height or position vector with correct \mathbf{j} component $(\mathbf{i} + 500 \ \mathbf{j})$ A1: Correct height stated. Condone 500 \mathbf{j} .
(b)	$\mathbf{v}(20) = (4.2\mathbf{i} + 2.5\mathbf{j}) \times 20$ = $84\mathbf{i} + 50\mathbf{j}$	M1 A1	2	M1: Using $\mathbf{v} = \mathbf{u} + \mathbf{a}t$ to find the velocity at $t = 20$ with $\mathbf{u} = 0\mathbf{i} + 0\mathbf{j}$. A1: Correct velocity.
(c)	$1.25t^{2} = 180$ $t = \sqrt{\frac{180}{1.25}} = 12 \text{ s}$ $\mathbf{v} = (4.2\mathbf{i} + 2.5\mathbf{j}) \times 12$ $= 50.4\mathbf{i} + 30\mathbf{j}$ $v = \sqrt{50.4^{2} + 30^{2}} = 58.7 \text{ ms}^{-1}$ OR $a = \sqrt{4.2^{2} + 2.5^{2}} = 4.89$ $v = 4.89 \times 12 = 58.7 \text{ ms}^{-1}$	M1A1 A1 dM1 A1 dM1A1 (dM1A1) (dM1A1)	7	M1: Equation based on height of 180 to find <i>t</i> . A1: Correct equation. A1: Correct <i>t</i> . dM1: Using v = u + a <i>t</i> to find the velocity at their time with u = 0 i + 0 j . A1: Correct velocity. dM1: Finding speed from their velocity. A1: Correct speed. Accept 58.6 or AWRT 58.7. dM1: finding magnitude of acceleration. A1: correct magnitude. dM1: acceleration × 12. A1: correct speed.
	OR $x = 4.2 \times \frac{180}{2.5} = 302.4$ $v_x = \sqrt{2 \times 4.2 \times 302.4} = 50.4$ $v_y = \sqrt{2 \times 2.5 \times 180} = 30$ $v = \sqrt{50.4^2 + 30^2} = 58.7$	(M1A1) (dM1A1) (A1) (dM1A1)		M1: finding horizontal displacement when height is 180. Must see 4.2, 2.5 and 180. May be implied by seeing 302.4. A1: Seeing 302.4 dM1: Finding both components of velocity. A1: Seeing 50.4. A1: Seeing 30. dM1: Finding the speed. A1: Final answer of 58.7

Q	Solution	Marks	Total	Comments
7(c) cont	$ \begin{array}{l} OR \\ v_y = \sqrt{2 \times 2.5 \times 180} = 30 \end{array} $	(M1A1)		M1: Equations based on height of 180 to find <i>v</i> and then <i>t</i> .
	$30 = 0 + 2.5t$ $t = \frac{30}{2.5} = 12$ $v_x = 0 + 4.2 \times 12 = 50.4$ $v = \sqrt{50.4^2 + 30^2} = 58.7 \text{ ms}^{-1}$	(A1) (dM1A1) (dM1A1)		A1: Correct equation for <i>t</i> . A1: Correct <i>t</i> . dM1: Using $v = u + at$ to find the j component of velocity at their time with $u = 0$. A1: Correct velocity. dM1: Finding speed from their velocity. A1: Correct speed. Accept 58.6 or AWRT
	OR			58.7.
	$\tan^{-1}\left(\frac{2.5}{4.2}\right) = 30.76^{\circ}$ $v_{v} = \sqrt{2 \times 2.5 \times 180} = 30$ $v = \frac{30}{\sin 30.76} = 58.7 \text{ m s}^{-1}$	(M1A1) (A1) (dM1A1) (dM1A1)		 M1: Finding angle using acceleration components. A1: Correct expression for acceleration components A1: Correct angle. dM1: Finding v_y at height of 180
	Total		12	A1: Correct speed of 30. dM1: Using trig to get <i>v</i> . A1: Correct speed. Accept 58.6 or AWRT 58.7.

Q	Solution	Marks	Total	Comments
8(a)	$\tan \alpha = \frac{6}{10}$			M1: Using tan with 10 and 5 or 6, OR sin
	$\tan \alpha = \frac{10}{10}$	M1		or cos with $\sqrt{136}$ and 6 or 10, OR sin or
	$\alpha = 31.0^{\circ}$	A1	2	cos with $\sqrt{125}$ and 5 or 10.
			2	Note: $\sin \alpha = \frac{6}{\sqrt{136}}$ and $\cos \alpha = \frac{10}{\sqrt{136}}$ A1: Correct angle. Accept 30.9° or AWRT 31°
(b)	$8 \sin \alpha t + 4.9t^{2} = 6$ $4.9t^{2} + 4.116t - 6 = 0$ $t = 0.76359 \text{ or } t = -1.60 \text{ s}$ $t = 0.764$	M1 A1FA1F A1 dM1 A1	6	M1: equation for the vertical motion containing ± 6 or ± 5 , $\pm 4.9t^2$ and $\pm 8\sin\alpha$ or $\pm 8\cos\alpha$, where α has a value related to their answer to part (a) (May be a negative angle). A1F: Correct terms. A1F: Correct signs and terms Follow through angle from part (a). A1: Correct equation rearranged equal to zero, but may be implied by subsequent working. dM1: Attempting to solve their quadratic equation. Only award method mark if method seen or correct answers obtained or -0.764 with $+1.60$. A1: Correct solution obtained. Accept
	OR			0.763 or AWRT 0.764.
	$v = \sqrt{(8\sin 31.0^{\circ})^{2} + 2 \times 9.8 \times 6} = 11.60$ $11.60 = 8\sin 31^{\circ} + 9.8t$ $t = \frac{11.60 - 8\sin 31^{\circ}}{9.8} = 0.763$	(M1) (A1FA1F) (dM1) (A1) (A1)		M1: Use a constant acceleration equation $v^2 = u^2 + 2as$ to find v . A1F: Correct equation. A1F: Correct v . dM1: Use of $v = u + at$ to find t A1: Correct equation. A1: Correct t (0.763)
(c)	$d = 10 - 8\cos\alpha \times 0.764$ $= 10 - 5.238$ $= 4.76 \text{ m}$	M1dM1 A1 A1	4	M1: Finding a horizontal distance using 8cosα or 8sinα multiplied by their time from part (b). dM1: For subtracting their distance from 10. A1: Seeing AWRT 5.24 or 5.23 from 0.763. A1: Correct final answer. Accept AWRT 4.76. Accept 4.77 from use of 0.763.
	Total		12	
	TOTAL		75	